Mapping Conceptual to Logical Models for ETL Processes

Alkis Simitsis
National Technical University of Athens
asimi@dbnet.ece.ntua.gr

ABSTRACT
Extraction-Transformation-Loading (ETL) tools are pieces of software responsible for the extraction of data from several sources, their cleansing, customization and insertion into a data warehouse. In previous line of research, we have presented a conceptual and a logical model for ETL processes. In this paper, we describe the mapping of the conceptual to the logical model. First, we identify how a conceptual entity is mapped to a logical entity. Next, we determine the execution order in the logical workflow using information adapted from the conceptual model. Finally, we provide a methodology for the transition from the conceptual to the logical model.

Categories and Subject Descriptors
H.2.1 [Database Management]: Logical design - data models, schema and subschema.

General Terms
Algorithms, Design.

Keywords
Data warehousing, ETL, conceptual modeling, logical modeling.

1. INTRODUCTION
Our goal is to provide a methodology for facilitating the modeling and management of ETL (Extraction-Transformation-Loading) processes. In previous works [14, 15], we have presented a generic multilevel modeling framework for ETL processes. In this paper, we bridge the different levels of our framework by presenting a semi-automatic transition from conceptual to logical model for ETL processes. By relating a logical to a conceptual model, we exploit the advantages of both worlds. On one hand, there exists a simple model, sufficient for the early stages of the data warehouse design. On the other hand, there exists a logical model that offers formal and semantically founded concepts to capture the characteristics of an ETL process.

Although there are several research approaches concerning the (semi-)automation of several tasks of logical DW design from conceptual models [1, 2, 3, 4, 7, 8, 9], so far, we are not aware of any other research approach concerning a mapping from a conceptual to a logical model for ETL processes. During the transition from one model to the other we have to deal with several issues. First, we need to identify the correspondence between the two models. Since the conceptual model is constructed in a more generic and high-level manner, each conceptual entity is mapped to a logical entity; however, the opposite does not hold. In the sequel, for each conceptual construct we provide its respective logical entity and we describe a method for the automatic transition from the former to the latter.

Moreover, we go beyond the simple one-to-one mapping and we combine information for more than one conceptual construct in order to achieve a better definition for a logical entity. For example, the conceptual entity ‘transformation’ is mapped to a logical ‘activity’. However, it is not obvious how the activity is fully described by the conceptual information provided. Using the conceptual schemata (input and output) of the transformation and its provider source, one can identify the schemata of the respective activity either directly (input, output and functionality) or indirectly (generated and projected-out). Still, this is insufficient, because we do not get any information about the instantiation of the appropriate template activity. As we show later in this paper, this issue can be addressed using extra information adapted from a note attached to the conceptual transformation.

The conceptual model is not a workflow; instead, it simply identifies the mappings and the transformations needed in an ETL process. The placement of the transformations into the conceptual design does not directly specify their execution order. However, the logical model represents a workflow and thus, it is very important to determine the execution order of the activities. To tackle this, we provide a method for the semi-automatic determination of a correct execution order of the activities in the logical model, wherever this is feasible, by grouping the transformations of the conceptual design into stages of order-equivalent transformations.

Finally, with the goal of formalizing the mapping between the two models and dealing with the aforementioned problems, we present a sequence of steps that constitutes the methodology for the transition from the conceptual to the logical model.

In summary, the contribution of this paper lies in:

- The representation of the conceptual constructs in terms of the logical formal definitions.
- The determination of the execution order of the activities in the logical workflow.
- The presentation of a methodology for the transition from the conceptual to the logical model.

Outline. The paper is organized as follows. In Sections 2 and 3, we briefly describe the main characteristics of the conceptual and logical models respectively. In Section 4, we discuss the mapping of each conceptual entity to a logical one. In Section 5, we present a semi-automatic determination of the execution order of the activities in the logical workflow. In Section 6, we provide a
methodology for the realization of the mapping between the two models. In Section 7, we present related work. Finally, in Section 8 we conclude our discussion with a prospect to the future.

An extended version of this paper can be found in [10].

2. CONCEPTUAL MODEL (abridged)

In this section, we focus on the conceptual part of the definition of the ETL process. For a detailed presentation of our conceptual model and formal foundations for the representation of ETL processes, we refer the interested reader to [11, 15].

Example. To motivate our discussion we introduce an example involving two source databases S1 and S2 as well as a central data warehouse DW. The scenario involves the propagation of data from the concept PARTS of source S1 as well as from the concept PARTS of source S2 to the data warehouse. In the data warehouse, DW.PARTS stores daily (DATE) information for the available quantity (QTY) and cost (COST) of parts (PKEY). We assume that the first supplier is European and the second is American, thus the data coming from the second source need to be converted to European values and formats. For the first supplier, we need to combine information from two different tables in the source database, which is achieved through an outer join of the concepts PS1 and PS2; respectively. Also, there exist two data sources, files RecentParts and AnnualParts, which contain information on daily and annual base respectively, for the population of the second supplier. In Figure 1, whose elements are explained in the following, we depict the full fledged diagram of the example, in terms of our conceptual model. In Figure 2, we graphically depict the different entities of the proposed model.

### Figure 1. Conceptual design of our example

The main entities of our model are the following.

Attributes. Attributes are the granular module of information. Their role is the same as in the standard ER/dimensional models (e.g., PKEY, DATE, COST, etc.).

Concepts. A concept represents an entity in the source databases or in the data warehouse (e.g., S1.PARTS, DW.PARTS).

Transformations. Transformations are abstractions that represent parts, or full modules of code, executing a single task and include two large categories: (a) filtering or data cleaning operations (e.g., not null (NN) check); and (b) transformation operations, during which the schema of the incoming data is transformed (e.g., surrogate key assignment (SK) transformation).

ETL Constraints. They are used in several occasions when the designer wants to express the fact that the data of a certain concept fulfill several requirements (e.g., to impose a PK constraint to DW.PARTS for the attributes PKEY and DATE).

### Notes

Notes are used to capture extra comments that the designer wishes to make during the design phase or render constraints attached to an element or set of elements. A note in the conceptual model represents: explanations of the semantics of the applied functions, and/or simple comments explaining design decisions or constraints. We consider that the information of a note which is classified into the former category indicates either the type or an expression/condition of a function and it is attached to a transformation or an ETL constraint. The information of a note of the second category is simple text without special semantics; these notes are used to cover different aspects of the ETL process, such as the time/event based scheduling, monitoring, logging, error handling, crash recovery etc. Formally, a note is defined by: (a) a name, and (b) a content, which consists of one or more clauses of the form: \(<\text{type}>::<\text{text}>\).

We discriminate three different types of information (clauses) in the content of a note using a simple prefix: (a) \(f::\) for a function type; (b) \(e::\) for an expression; and (c) \(t::\) for simple text, before writing the text of the respective information. In order to maintain our model simple, we do not oblige the designer to attach a note to every transformation or ETL constraint, or to fill all three types of information in every note.

In Figure 1 observe several notes of the first category attached to transformations \(f_1, f_2, f_3,\) and \(\triangleright\). For example, the note attached to the transformation \(\triangleright\), indicates that the type of the transformation template is outer join and the expression needed for its instantiation is \(PS1.PKEY+PS2.PKEY\).

Part-of Relationships. Part-of relationships emphasize the fact that a concept is composed of a set of attributes, since we need attributes as first class citizens in the inter-attribute mappings.

Candidate relationships. A set of candidate relationships captures the fact that a certain data warehouse concept (e.g., source table \(S_1\)) can be populated by more than one candidate source concepts (e.g., source files AnnualParts and RecentParts).

Active candidate relationships. This relationship denotes the fact that out of a set of candidates, a certain one (e.g., RecentParts) has been selected for the population of a concept.

Provider relationships. A 1:1 (N:M) provider relationship maps a (set of) input attribute(s) to a (set of) output attribute(s) through a relevant transformation.

Transformation Serial Composition. The composition is used when we need to combine several transformations in a single provider relationship (e.g., the combination of \(S\) and \(\gamma\)).

The proposed model is constructed in a customizable and extensible manner, so that the designer can enrich it with his own re-occurring patterns for ETL activities, such as the assignment of surrogate keys or the check for null values.
3. LOGICAL MODEL (abridged)

In this section, we present a condensed version of the logical model for ETL workflows that concentrates on the flow of data from the sources towards the data warehouse through the composition of activities and data stores. The full-blown version and the formal representation of the model can be found in [14].

The full layout of an ETL workflow, involving activities, recordsets and functions can be deployed along a graph in an execution sequence that can be linearly serialized. We call this graph, the Architecture Graph. The graphical notation for the Architecture Graph is presented in Figure 3.

As we have already stressed, since the conceptual model is constructed in a more generic and high-level manner, not all the logical entities have a mapping to a conceptual entity. In the logical modeling some entities are used in order to capture more detailed semantics of the logical design, e.g., the derived provider relationships, which can be determined only after the deliverable of this mapping has been produced. Thus, here we present only the logical entities that can be mapped to a conceptual entity. In this setting, the components of our modeling framework are:

- **Attributes**: They are characterized by their name and data type.

- **Recordsets**: A recordset is characterized by its name, its (logical) schema and its (physical) extension (i.e., a finite set of records under the recordset schema).

- **Elementary Activities**: They are logical abstractions representing parts, or full modules of code. An **Elementary Activity** (simply referred to as **Activity** from now on) is formally described by the following elements:
  - **Name**: a unique identifier for the activity.
  - **Input Schemata**: a finite list of one or more input schemata that receive data from the data providers of the activity.
  - **Output Schemata**: a finite list of one or more output schemata that describe the placeholders for the rows that pass the checks and transformations performed by the activity.
  - **Functionality Schema**: a finite list of the attributes which take part in the computation performed by the activity (in fact, these are the parameters of the activity).
  - **Generated Schema**: a finite list of attributes, belonging to the output schema(ta), that are generated due to the processing of the activity.
  - **Projected-Out Schema**: a finite list of attributes, belonging to the input schema(ta), that are not further propagated from the activity.
  - **Operational Semantics**: a program, in LDL++ [16], describing the content passing from the input schemata towards the output schemata. For example, the operational semantics can describe the content that the activity reads from a data provider through an input schema, the operation performed on these rows before they arrive to an output schema and an implicit mapping between the attributes of the input schema(ta) and the respective attributes of the output schema(ta).

- **Execution priority**: In the context of a scenario, an activity instance must have a priority of execution, determining when the activity will be initiated.

- **Provider** relationships. These relationships capture the mapping between the attributes of the schemata of the involved entities.

- **Part_of** relationships. These relationships involve attributes and parameters and relate them to their respective activity, recordset or function to which they belong.

Figure 4 depicts a simplified (on account of the limited space) diagram of the example of Figure 1, in terms of our logical model.

Similarly to the templates of the conceptual model, we offer an extensible palette of templates to the logical model too [14].

4. MAPPINGS

In this section, we examine one by one the constituents of the conceptual model, we identify their respective logical entities, and we describe how each conceptual entity is mapped to a logical one. Concepts and attributes are mapped to recordsets and attributes. Transformations and ETL constraints are mapped to activities. Notes are used for the determination and instantiation of the appropriate template activity. Moreover, we tackle two special design cases: the case of projected-out attributes, and the convergence of two separate data flows at a common data store.

4.1 Concepts and Attributes

One of the main tasks of the conceptual model is to identify all data stores, along with their attributes, involved in the whole ETL process. For each concept in the conceptual model, a recordset is defined in the logical. The name and the list of attributes of the recordset are the same with those of the concept. There is one-to-one mapping from each attribute of the conceptual model to a respective one in the logical model; i.e., its name and data type remain the same. Figure 5 depicts the transition of concepts S1.PARTS and DW.PARTS to the respective recordsets along with its attributes.

4.2 Relationships

The conceptual model consists of four kinds of relationships: part-of, candidate, active candidate, and provider relationships.

The part-of relationships are used to denote the fact that a certain concept comprises a set of attributes; i.e., that we treat attributes as ‘first-class citizens’ in our model. We maintain this characteristic in the logical model too; thus, the conceptual part-of relationships are mapped to logical part-of relationships, with exactly the same semantics and characteristics. Observe the usage of part-of relationships in Figure 5.
The candidate and the active candidate relationships are not directly mapped to logical model. Their introduction in the conceptual model covers the usual case that in the early stages of the data warehouse design there may exist more than one candidate concepts (data stores) for the population of a certain concept. When we move on to the logical design, these problems have already been solved at the previous steps of the lifecycle [11]. Therefore, we only need to transform the active candidate concept; i.e., the one that is chosen, to a logical recordset.

The provider relationships intuitively represent the flow of data during an ETL process. Consequently, a conceptual provider relationship between a source and a target attribute involves all the transformations that should be applied according to design requirements. In the absence of any transformation between a source and target, the conceptual provider relationship can be directly mapped to a logical provider relationship (Figure 5).

![Figure 5. Transition of a simple provider relationship](image)

The case where one or more transformations are needed between source and target attributes is covered in the next subsection.

### 4.3 Conceptual Transformations

In the conceptual model, we use transformations in order to represent tasks that either (a) maintain the schema of data (e.g., cleansing, filtering); in general, we name these transformations filters, or (b) change the schema of data (e.g., aggregation); we name these transformations transformers. In the logical level, we use activities to represent the same tasks. Thus, the mapping of conceptual to logical model includes the mapping of conceptual transformations to logical activities.

By observing the characteristics of the logical model and comparing the nature of its constructs to the constructs of the conceptual model, we understand that in order to fully describe the mapping between transformations and activities, we have to deal with three main issues:

- The specification of the properties of an activity (e.g., name, schemata, semantics).
- The serial composition of conceptual transformations.
- The definition of the execution order of activities in the logical model.

In this subsection, we are dealing with the last two issues. The latter is discussed later in the paper.

**Properties of an activity.** Formally, a transformation T in the conceptual level (either a filter or a transformer) is mapped to an activity A in the logical level. The input attributes of T comprise the functionality schema of the respective activity A (A.fun). If there are attributes belonging to the output schema of T that do not have a consumer in the output schema of T, then these attributes comprise the projected-out schema of the activity (A.pro).

In the simplistic case of an ETL process that involves only one transformer, the attributes of the source concept (let’s say S1) of T comprise the input schema of activity A (A.in) and the attributes of the target concept (let’s say S2) of T comprise the output schema of activity A (A.out). So the following formulae are valid:

\[
\begin{align*}
A.\text{in} &= S_1.\text{out} \\
A.\text{out} &= S_2.\text{in} \\
A.\text{fun} &= T.\text{in} \\
A.\text{pro} &= T.\text{in} - T.\text{out}
\end{align*}
\]

Obviously, for filters A.gen=Ø and A.pro=Ø hold. Figure 6 depicts an example of the determination of activity’s schemata for a transformer.

![Figure 6. Mapping of a transformer T to an activity A](image)

Note that in more complex cases, the input and output schemata are not computed so easily. In [12], we discuss how we confront such cases and we present an algorithm called Schema Generation that automates the creation of all input and output schemata involved in the whole ETL process.

**Serial Composition.** In the conceptual model, when we need to combine several transformations in a single provider relationship (e.g., the combination of SK1 and γ in Figure 1), we apply a serial composition. The mapping of the serial composition to the logical model is quite straightforward. The serial composition of the two transformations T1 and T2 is mapped to a sequence of two activities A1 and A2 in the logical level. The execution order of the two activities is determined from the order of the respective transformations in the serial composition. The schemata of the two activities are defined as we have already seen. The only difference is that the output schema of the initial activity A1 will populate the input schema of the subsequent activity A2, i.e.,

\[
A_1.\text{in}=A_2.\text{out}.
\]

### 4.4 Transformation of Notes

So far, we have described how the schemata of an activity, along with the appropriate inter-attribute mappings are determined. The next issue towards the complete description of an activity is the identification of its operational semantics; i.e., the appropriate LDL++ program that describes its operation. In previous work [14], we have provided a generic and extensible palette of template activities, and we have presented how the expression of an activity, which is based on a certain simple template, is produced by a set of LDL++ rules of the following form that we call Template Form:

\[
\text{OUTPUT}() \leftarrow \text{INPUT}(), \text{EXPRESSION}, \text{MAPPING}.
\]

Clearly, the OUTPUT, INPUT and MAPPING parts of the above form have been already covered by the mapping of a conceptual transformation to a logical activity presented before. Here, we
concretely describe (a) how the designer chooses a template activity, and (b) what the EXPRESSION part is.

To succeed in this task, we take advantage of the usage of the notes attached to transformations. After parsing the information of a note, we get extra information concerning the transformation involved: (a) its function type (clause f::); (b) the expression(s) needed for the instantiation of its function type (clause e::); and, (c) design decisions or constraints (clause t::).

Using the type provided by the f:: clause, we chose a template activity from a template library. In the case that no template of such type exists in the library, the designer can either register a new one or solve this problem later in the logical design. In each template there are one or more parts that should be determined during its instantiation. This job is facilitated by the e:: clause. A properly completed e:: clause indicates the requisite expression(-s) for a template. If more than one predicate is used in the template definition; i.e., it is a program-based template [14], then it is possible that more than one expression will be required. Also, even a single predicate template is possible to have more than one expression in its definition. In such cases, the respective note should provide all the expressions needed in the order they should be placed into the template definition. If a note does not contain all the appropriate expressions or if it does not contain them in the right order or even if it contains them not properly completed, then the template activity can not be automatically constructed and further interference from the designer is required.

For instance, consider the transformation f1 depicted in Figure 1. This transformation represents a function tagged by a note that provides twofold information about: (a) its type: f::addAttribute; and (b) its required EXPRESSION: e::DATE=SYSDATE. Figure 7 shows how to use this information to instantiate the operational semantics of activity f1. We use the f:: information to choose the appropriate template for the logical activity. Thus, the conceptual transformation f1 is mapped to the logical activity f3 whose operational semantics are determined by the template activity addAttribute (1st row). The EXPRESSION part of addAttribute is @OUTFIELD = @VALUE; i.e., the new attribute (OUTFIELD) takes an initial value (VALUE). For transformation f3, the EXPRESSION is: e::DATE=SYSDATE. After the parameter instantiation (2nd row) we get the operational semantics of the activity f3 (3rd row).

| Template | a_out((OUTPUT_SCHEMA, @OUTFIELD) <- a_in1(INPUT_SCHEMA), @OUTFIELD = @VALUE, DEFAULT_MAPPING. |
| Parameter instantiation | @OUTFIELD = DATE @VALUE = SYSDATE |
| Operational semantics of activity f3 | f3_out(PKEY_out, QTY_out, COST_out, DATE) <- f3_in1(PKEY_in, QTY_in, COST_in), PKEY_out = PKEY_in, QTY_out = QTY_in, COST_out = COST_in. |

**Figure 7. Operational semantics of activity f3**

For further information concerning the usage of function types, templates, and expressions we refer the interested reader to [14].

In the conceptual model, the population of a concept (e.g., DW.PARTS) from more than one source is abstractly denoted by provider edges that simply point at this concept. The logical model, that is more rigorous, needs a more specific approach to cover the population of a recordset from more than one source. A solution to this is the addition of an

**4.5 Transformation of ETL Constraints**

In the conceptual model, ETL Constraints are used to indicate that the data of a certain concept fulfill several requirements. For instance, in Figure 1 we impose a PK constraint to DW.PARTS for the attributes PKEY and DATE. The functionality of an ETL constraint is semantically described from the single transformation that implements the enforcement of the constraint. Thus, we treat conceptual ETL constraints as the conceptual transformations and we convert them to logical activities. More specifically, each ETL constraint enforced to some attributes of a concept S1 is transformed to an activity A that takes place in the logical workflow exactly before the respective recordset S1 that stands for the concept S1. The schemata of the activity are filled in the same manner and under the same procedures as in the case of the mapping of conceptual transformations. The finite set of attributes of S1, over which the constraint is imposed, constitutes the functionality schema of A. The input and output schemata of A comprise of all the attributes of S1.

**4.6 Special Cases**

In this subsection, we tackle two special design issues that arise in the mapping of conceptual to logical model.

**Rejection of an attribute.** During an ETL process some source attributes may be projected-out from the flow. We discriminate two possible cases:

- An attribute that belongs to the schema of a concept. This case is covered by the conceptual model as an attribute that has not an output provider edge (e.g., in Figure 1, the attribute S2.PARTS.DEPT is not further propagated towards DW).

- An attribute that participates in a certain transformation but it is not further propagated. This case is covered by the conceptual model as an attribute that belongs to the input schema of a transformation, but there is not an output edge tagged with the name of the discarded attribute from the transformation to any attribute (e.g., in Figure 1, the attribute S1.PARTS.DEPT participates to the outer join, but is not further propagated towards S1.PARTS).

In the mapping of conceptual to logical, the first case is handled with the addition of an extra activity that projects-out the appropriate attribute(s); this activity should be placed immediately after the respective recordset.

On the other hand, the second case should not be examined as a special case. The reason behind this is that the inter-activity discarding of attributes is captured by the semantics of the activity and the attributes discarded are simply belonging to the projected-out schema of the activity. Thus, this case is covered by the conversion of conceptual transformations to logical activities.

**Convergence of two flows.** In the conceptual model, the population of a concept (e.g., DW.PARTS) from more than one source is abstractly denoted by provider edges that simply point at this concept. The logical model, that is more rigorous, needs a more specific approach to cover the population of a recordset from more than one source. A solution to this is the addition of an
extra activity that unifies the different flows. Therefore, the convergence of two (or more) flows is captured in the logical model with the usage of a union (U) activity. Obviously, before the addition of a union activity, each of the involved flows populates the same data store, i.e., the same schema. Thus, the input schemata of the union activity are identical. Since a union has empty functionality, generated and projected-out schemata, its output schema is the same with any of its input schemata and also, it is the same with the schema of the target recordset.

5. EXECUTION ORDER

So far, we have clarified how from the conceptual model of an ETL process, one can: (a) identify the concerned data stores; (b) pick out the transformations that need to take place in the overall process; and (c) describe the inter-attribute mappings. But a further, more detailed, study of the data flow generates some questions concerning the execution order of the activities in the logical workflow. Consider the part of Figure 1 that involves the population of DW.PARTS from S2.PARTS. In order to design a logical workflow for this example, we have to answer questions like ‘Q1: which of the activities SK1 and γ should precede?’ or ‘Q2: which of the activities SK1 and f1 should precede?’.

This section presents a method for determining the execution order of activities in the logical workflow. At first, without loss of generality, we examine the simplistic case of the population of a target concept from one source. With the intention of classifying the transformations according to their placement into the design, we define transformation stages and we give an algorithm for finding them. Also, we discuss issues concerning the ordering of transformations included in the same stage. Afterwards, we extend this method to capture more complex and realistic cases involving more than two data stores.

5.1 Stages

Assume the case of simple ‘one source-one target’ flow, like the example depicted in Figure 8. The motivating question Q1 can be answered by some quick observations in Figure 8. Since the transformation γ has input attributes that belong to the output schema of SK1, f1 and f2, it should follow them at the logical level. For a similar reason, the activity σ should follow γ. Moreover, after the presentation of the special cases in subsection 4.6, we should also take into account two more activities: (a) the ETL constraint PK; recall that when we transform an ETL constraint into an activity, we should place it exactly before the recordset involved (DW.PARTS); and (b) the ‘hidden’ activity that projects-out the attribute DEPT; recall that this activity should be placed exactly after the source concept (S2.PARTS).

Intuitively, one can divide the design into several groups of transformations (Figure 8), mainly due to the following observations:

- the position of some activities in the workflow can be figured out, by detecting their providers and consumers, and
- extra activities can be placed in the workflow, by applying the mapping rules for ETL constraints and special cases.

The aforementioned observations guide us to divide the design into several transformation stages. A transformation stage (or a stage) is a visual region in a ‘one source-one target’ conceptual design that comprises (a) a concept and its attributes (either the source or the target concept), or (b) a set of transformations that act within this region. A stage is shown as a rectangle labeled at the bottom with a unique stage identifier: an auto-incremental integer with initial value equal to 0, where stage 0 comprises only the source concept.

Assume two conceptual transformations T1 and T2. Then, the execution order of their respective activities A1 and A1 in the logical model is computed as follows. When T1 belongs to a stage with smaller identifier than the stage of T2, then A1 has smaller execution priority (i.e., it is executed prior) than A2.

Up to now, we have answered the first motivating question. Another issue that remains to be clarified is the determination of the execution priority among transformations that belong to the same stage. The transformations that belong to the same stage are called stage-equivalent transformations.

![Figure 8. Transformation stages](image-url)

We tackle this problem using the following thought. If all activities that stem from stage-equivalent transformations are swappable, then there is not a problem in their ordering. Consequently, we answer questions concerning the ordering of activities of this kind, by studying which of these activities can be swapped with each other. For the rest of activities, extra action from the designer is needed.

In [12] we resolve the issue of when two activities can be swapped in a logical ETL workflow, i.e., when we are able to interchange their execution priorities. Also, we provide a formal proof that the swapping of two activities A1 and A2 is allowed, when the following conditions hold:

1. A1 and A2 are adjacent in the graph; without loss of generality assume that A1 is a provider for A2.
2. both A1 and A2 have a single input and output schemata and their output schema has exactly one consumer
3. the functionality schema of A1 and A2 is a subset of their input schema, both before and after the swapping
4. the input schemata of A1 and A2 are subsets of their providers, again both before and after the swapping

All stage-equivalent transformations could be adjacent and this is valid for their respective activities too; thus condition (1) holds. Since stages are defined between two concepts, in a single stage all transformations, as well as their respective activities, have a single input schema and a single output schema; thus condition (2) holds too. Therefore, we have to examine the validity of
conditions (3) and (4), in order to decide if two transformations belonging to the same stage are swappable or not.

The transformations that belong to the same stage, and whose respective activities in the logical design are swappable, are called order-equivalent transformations. For two order-equivalent transformations \( A_i \) and \( A_{i+1} \); the following formulae hold:

\[
A_i . fun \subseteq A_i . in \\
A_i . in \subseteq A_{i+1} . out
\]

The above formulae represent the conditions (3) and (4) respectively. If these formulae do not hold for two stage-equivalent transformations, then we cannot automatically decide their order and we need additional information from the user.

Clearly, this extra information is required only in cases of bad design [10]. As we have already stressed out [15], we do not provide any strict verification method for the conceptual model. This decision lies on our choice to provide a simple model with its main purpose to be the identification of the data stores and transformations involved in the overall ETL process. This model is addressed not only to administrators, but also to managers and people with low expertise in data warehousing, in order to make these totally different groups to understand each other using a simple design language. Therefore, we allow cases of bad conceptual design, given that when the deliverable of this stage propagates to the next level (the logical design) it will be replenished and corrected wherever needed.

### 5.2 Stage Derivation

We now present the FS algorithm (Figure 9) that is used for the automatic determination of all stages of a conceptual design which involves a source and a target concept. The FS algorithm accomplishes the following tasks: (a) first, it finds out all the attributes that should be projected-out in the terms introduced for the conceptual model. (b) then, it divides the design into several attributes that should be projected-out in the terms introduced in subsection 4.6; and (b) then, it divides the design into several attributes that should be projected-out in the terms introduced in subsection 4.6, (c) then, it returns the set of all transformations between \( C_s \) and \( C_t \).

#### Algorithm Find Stages (FS)

1. **Input**: A graph \( G_p = (V', E') \), where \( V' \) contains a source concept \( C_s \), a target concept \( C_t \), their attributes, and a set \( AT \) of all transformations between \( C_s \) and \( C_t \).
2. **Output**: An array \( Stage_{C_s, C_t}[id], id=0, ..., n \), where \( n \) is the number of all possible stages between \( C_s \) and \( C_t \).
3. **Begin**
4. \( id = 0 \);
5. \( Stage[id] = \{C_s\} \);
6. \( id++ \);
7. **for each** attribute \( a_i \in C_s . out \) {
8. if ( \( \forall x \in V' - C_s \), \( \neg \)edge \((a_j, x)\) ) {
9. \( Stage[id] = \{n - out_b\}; \)
10. }
11. **while** (\( AT \neq \emptyset \) ) {
12. \( id++ \); //a new id for a new stage
13. **for each** transformation \( T_i \in AT \) {
14. if ( \( \forall a_j \in T_i . in \), \( \exists \) node \( V \in Stage[id-k] \), \( k=1, ..., id \), s.t. \( a_j \in V . out \) ) {
15. \( AT = AT - \{T_i\} \);
16. \( Stage[id] = Stage[id] \cup \{T_i\} \);
17. }
18. \( Stage[++id] = \{C_t\} \);
19. return Stage[];
20. **End.**

Figure 9. The FS algorithm

#### 5.3 Stages in Designs Involving Binary Transformations

Up to now, we have dealt with simple ‘one source-one target’ ETL processes. We extend this assumption by taking into account the binary transformations that combine more than one flow. In this case, we follow a threefold procedure for finding the execution order of the activities in the overall workflow: (a) we compute the stages of each separate ‘one source-one target’ flow; (b) we construct the linear logical workflows; and (c) we unify them into one workflow. The union of two workflows is realized on their common node; i.e., either a recordset or a binary transformation, which is called the joint-point of the two workflows. As we have already discussed in subsection 4.6, if the joint-point is a data store then for the convergence of two workflows we need an extra union activity (U) that should be placed exactly before the joint point; i.e., the common data store. If the joint-point is a binary transformation then we simply unify the two flows on that node.

At first, we give an intuitive description of how we deal with complex designs involving more than one source, and then we present an algorithm for the formal finding of stages in such complex designs.
Without loss of generality, assume the case of ‘two sources-one target’ flow. Obviously, for each binary transformation $T_b$, there are two providers and one consumer. These three entities can be either concepts or transformations depending each time from the position of $T_b$ in the workflow. Assume the case of the population of a target data store $DW$ from two source data stores $S_1$ and $S_2$ (Figure 10(a)) through several unary transformations and one binary transformation $T_b$. We use an incremental technique for the design of the logical workflow. At first, we compute $Stage_{S1,DW}$ and $Stage_{S2,DW}$ that contain the stages of the ‘one source-one target’ flows defined by the two pairs of concepts $S_1$-$DW$ and $S_2$-$DW$. To find the appropriate order in the logical workflow when a binary transformation $T_b$ is involved, we select a) all the transformations that take place in the flow from the first source $S_1$ to the target concept $DW$; and b) a subset of the transformations from the second flow that consists of all the transformations between the second source concept $S_2$ and the binary transformation $T_b$. Thus, from $Stage_{S1,DW}$ we use all its elements:

$$Stage_{S1,DW}[i], i = 0, ..., n \text{ where } Stage_{S1,DW}[n] = \{DW\}$$

while from $Stage_{S2,DW}$ we use only the elements:

$$Stage_{S2,DW}[i], i = 0, ..., k \text{ where } Stage_{S2,DW}[k] = \{T_b\}$$

Finally, we unify the two flows on their joint-point, the activity $T_b$ (dashed arrow in Figure 10(b)).

**Figure 10. The case of a binary transformation**

The conviction that with the aforementioned technique we do not lose any transformation is supported by the following proposition.

**Proposition.** If two flows, $S_1$-$S_7$ and $S_2$-$S_7$ that involve the population of a target data store $S_7$ from two source data stores $S_1$ and $S_2$, respectively, have a binary transformation $T_b$ as a joint point, then the sub-flow $T_b$-$S_7$ is common in both initial flows.

The proof is straightforward, since, by definition, each transformation has one and only one output schema. Thus, the situation depicted in Figure 11 is unacceptable, because the only way to have different flows after a binary transformation is to allow it have two output schemas; and this is not valid.

**Figure 11. Problematic conceptual design**

Next, we present an algorithm for Finding Stages in Complex Conceptual Designs. The FSC algorithm (Figure 12) formally determines the execution order of activities in workflows that involve more than one source. It checks all the flows from each source to the target. It applies the $FS$ algorithm to each simple flow; i.e., to a flow that does not involve a binary transformation.

If the flow is complex, i.e., a flow that involves at least one binary transformation, then each time $FSC$ keeps track of binary transformations, and again, it applies the $FS$ algorithm.

The $FSC$ algorithm takes as input a directed graph that represents a conceptual design involving probably more than one source along with binary transformations. It checks all possible flows that could be created by any two concepts (Ln: 6). It becomes obvious from the aforementioned intuitive analysis, that the main goal is to find the boundaries of each flow. Clearly, we search only for the target of a flow, given that the source is always known. Initially, in each flow the first concept is the source and the second is the target (Ln: 7). If there does not exist any binary transformation in this flow then the target is still the second concept. If there exists a binary transformation $T_b$, then we confront this in a twofold way (Ln: 9-12). The very first time that we find $T_b$, we simply add it to a set, named visited $T_b$, and the ordering is determined from the whole flow. In the next appearance (or appearances, if we consider that a binary transformation can have more than two input schemata) of $T_b$, the second concept is not considered anymore as the target of the current flow checked; in this case we use the binary transformation $T_b$ as the target (Ln: 10). That is because the flow from $T_b$ towards the second concept has been determined before, at the first appearance of $T_b$. The set visited $T_b$ is used for storing every binary transformation counted so far in its first appearance.

**Algorithm Find Stages in Complex Conceptual Designs (FSC)**

1. **Input:** A graph $G=(V,E)$ that represents the whole conceptual design
2. **Output:** An array $LW[id], id=0,...,n$ where $n$ is the number of all possible logical workflows among concepts
3. **Begin**
4. visited $T_b = \{\}$
5. $id = 0$
6. for each pair $C_S,C_T$ 
7. Target $= C_T$
8. $AT = find\ all\ transformations(C_S,C_T)$
9. for each binary transformation $T_b \in AT$ 
10. if ( $T_b$visited $T_b$ ) ( Target $= T_b$ )
11. else { visited $T_b = visited\ T_b \cup \{T_b\}$; }
12. }
13. $LW[++id] = FS(G'C_S,TARGET; $$V'$$, $$E'$$), s.t. $$G'C_S$$ is the simple flow between $C_S$ and Target$}$
14. }
15. return $LW[]$
16. **End.**

**Figure 12. The $FS$ algorithm**

After having determined the target, we have fixed the boundaries of the flow that should be checked in order to determine the execution order of the logical activities. Once again, this is achieved through the application of the $FS$ algorithm to the flow between the source concept and the target chosen (Ln: 13). The $FS$ algorithm outputs the array Stage[] (see previous subsection) that contains the necessary information about the execution order of a certain flow. All arrays Stage[] of all the conceptual flows examined are stored in another array LW[].

When $FSC$ finishes, it returns the array $LW[]$ that contains all the individual simple flows that should be used to construct the logical workflow (Ln: 19). We should note here, that the term ‘construction’ refers to the determination of the placement
(execution order) of all data stores and transformation involved in the whole ETL process, rather than the whole composition of all constituents of the logical model.

5.4 Execution Order of Activities

So far, we have introduced stages and we have presented how these can be automatically identified in the conceptual design. We are ready now to describe how the execution order of activities in the logical design can be determined.

Usually, ETL processes consist of more than one ‘one source-one target’ flow, probably involving more than one binary activity. Thus, in general we should follow the technique described in the previous subsection for finding the execution order of activities involved in the overall process. At first, we find the proper execution order for every simple flow in the conceptual design, in order to establish the proper placement of the activities in linear workflows. Each of these workflows corresponds to one element of the LW[ ] array.

Algorithm Execution Order in Logical Workflows (EOLW)

1. Input: An array LW[id], id=0,...,n, where n is the number of all possible flows among concepts
2. Output: A graph G=(V,E) that represents the logical design
3. Begin
4. for each LW[i] in LW {
5. predecessor = LW[i].Stage[0];
6. V = V ∪ {predecessor};
7. for each Stage[j] in LW[i], j>0 {
8. predecessor = LW[i].Stage[j-1];
9. if (V ∩ E) { // if this is the first appearance of the node
10. V = V ∪ {predecessor};
11. E = E ∪ {predecessor,n};
12. }
13. }
14. if (V ∩ E) {
15. if (V ∈ E) { E = E ∪ {previous,n};
16. if (V ∈ RS) { // if it is a recordset
17. E = E ∪ (x,n) for all x ∈ E, where there is a RS association
18. V = V ∪ {U}; // add a Union activity
19. E = E∪{previous,U}∪(x,U)∪(U,n);
20. }
21. return G(V,E);
22. End.

Figure 13. The EOLW algorithm

The execution order of the activities in the logical workflow is determined by the EOLW algorithm. The EOLW algorithm (Figure 13) takes as input the array LW[ ] computed by FSC algorithm. Again, its main task is to construct the logical design, in terms of ‘filling’ places, rather than build the whole ETL process with its semantics; the latter is a later task presented in the next section. Thus, it creates and outputs a graph G(V,E) that contains all the necessary data stores and activities.

The procedure realized as follows. For every simple flow, i.e., for every element of LW[ ], algorithm EOLW processes all transformation stages, i.e., all elements of Stage[ ] (Lns 7-20). Each time it finds a new node, either data store or activity, it adds it to the graph along with an edge that connects this node with its prior in the flow (Lns 9-13). If a node has already been added in the graph then this is a case of convergence of two flows: the current one and the one already connected to this node (Lns 14). We discriminate two possible cases: the node is either a binary activity or a data store, i.e., it belongs to RS or A. The case of an already visited binary activity is the simplest; then, we need only a connection from its prior node in the current flow processed to the binary activity (Lns 15). The second case necessitates the usage of an extra Union activity (see subsection 4.6) placed exactly before the respective data store (Lns 16-20). To achieve this, we first delete the edge between the data store and the last node of the flow already connected to it (Lns 17). Then we add a new node representing the Union activity (Lns 18) and we connect it to both flows and the data store (Lns 19). Finally, EOLW returns the graph that represents the logical design.

6. METHODOLOGY

This section presents a sequence of steps that a designer should follow, during the transition from the conceptual to logical model, with the ultimate goal of the production of a mapping between the two models, along with any relevant auxiliary information.

Step 1: Preparation. We refine the conceptual and model in terms that no ambiguity is allowed. After we decide which the active candidate is, a simplified ‘working copy’ of the scenario that eliminates all candidates is produced [11]. Moreover, any additional information depicted as a note (e.g., comments, runtime constraints), which is not useful during the mapping, is discarded from the design, but it is recorded to a log file.

Step 2: Concepts and Attributes. Next, we add all necessary records along with their attributes. All concepts of the conceptual design are mapped to recordsets in the logical design. Similarly, their attributes are mapped to the attributes of the respective recordsets. Obviously, the part-of relationships remain the same after the transition from one model to the other.

Step 3: Transformations. After that, we determine the appropriate activities along with their execution order. Their determination is captured by the conceptual design: all transformations involved in the conceptual design are mapped to logical activities. Also, we incorporate activities that are not shown in the conceptual design, to capture the rejection of an attribute or the convergence of two flows. Afterwards, we determine the execution order of the activities, and we exploit the information provided by the notes to fully capture the semantics of every activity.

Step 4: ETL Constraints. The next step takes into account the ETL constraints imposed on the data stores. Recall that when we transform an ETL constraint into an activity, then we should place it exactly before the recordset involved. Thus, in this step, we enrich the logical design with extra activities that represent all ETL constraints of the conceptual design. To the extend that the execution order of these newly inserted activities is involved, we denote that the criteria of ordering are identical with those unfolded in the case of stage-equivalent transformations.

Step 5: Schemata Generation. As a final step, we should ensure that all the schemata involved in the overall process are valid. For this reason, we use the algorithm Schema Generation (SGen), introduced in [12], SGen automatically creates all the schemata involved in the logical design. The main idea of SGen is that after the topological sorting of an ETL workflow, the input schema of an activity is the same with the (output) schema of its provider and the output schema of an activity is equal to (the union of) its input schema(s), augmented by the generated schema, minus the
projected-out attributes. Therefore, for two subsequent activities $A_1$ and $A_2$, the following equalities hold:

$$A_1.\text{in} = A_1.\text{out}$$
$$A_2.\text{out} = A_2.\text{in} \cup A_2.\text{gen} - A_2.\text{proj}$$

Thus, given that the schemata of the source recordsets are known and the generated and projected-out schemata of each activity are provided by the template instantiation, the calculation of the schemata of the whole ETL process is feasible.

7. RELATED WORK

This section presents the state of the art concerning the correlation of two different levels of ETL design: conceptual and logical. Although, there exists several approaches [5, 6, 13, 15] for the conceptual part of the design of an ETL scenario, so far, we are not aware of any other research approach concerning a mapping from a conceptual to a logical model for ETL processes. However, there are some approaches concerning the (semi-) automation of several tasks of logical DW design from conceptual models. A number of approaches concern the development of dimensional models from traditional ER-models [1, 7]. In other approaches the data warehouse logical schema is generated from a conceptual schema. [8] presents a framework for generating a DW logical schema from a conceptual schema. [2] is an approach to derive initial data warehouse structures from the conceptual schemes of operational sources. [3] proposes a general methodological framework for data warehouse design, based on Dimensional Fact Model. [4] presents a modelling framework BabelFish concerning the automatic generation of OLAP schemata from conceptual graphical models and discusses the issues of this automatic generation process for both the OLAP database schema and the front-end configuration. [9] proposes algorithms for the automatic design of DW conceptual schemata.

8. DISCUSSION

Conclusions. In this paper we have presented a semi-automatic transition from a conceptual model to the logical model. First, we have identified the correspondence between the two models. Also, we have provided a method for the semi-automatic determination of a correct execution order of the activities in the logical model. Finally, we have presented a cohesive methodology that consists of a sequence of steps that a designer should follow, during the transition from the conceptual to logical model.

Correctness. Once again, our methodology is not a fully automatic procedure. This is due to the fact that intentionally we do not provide any strict verification method for the conceptual model [15]. The goal of this mapping is to facilitate the integration of the results accumulated in the early phases of a data warehouse project into the logical model, such as the collection of requirements from the part of the users, the analysis of the structure and content of the existing data sources along with their mapping to the common data warehouse model. Thus, the deliverable of this mapping could not necessary be a complete and accurate logical design. Hence, the designer during the mapping from the one model to the other or in the logical level, should examine, complement or change the outcome of this methodology.

Optimization. We note that the design of Figure 4 is not the only possible logical design that corresponds to the conceptual design of Figure 1. The constraints in the determination of the execution order require only that the placement of activities should be semantically correct or equivalently, that these activities can interchange their position without any semantic conflict. Clearly, $n$ order-equivalent activities can produce $n!$ different logical workflows. The final choice of one of them depends on other parameters beyond those examined in this paper; e.g., the total cost of a workflow. We have resolved this issue in [12], where we discuss optimization issues concerning the ETL processes.

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10. REFERENCES